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# Radiative forcing by contrails

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**Abstract.** A parametric study of the instantaneous radiative impact of contrails is presented using three different radiative transfer models for a series of model atmospheres and cloud parameters. Contrails are treated as geometrically and optically thin plane parallel homogeneous cirrus layers in a static atmosphere. The ice water content is varied as a function of ambient temperature. The model atmospheres include tropical, mid-latitude, and subarctic summer and winter atmospheres. Optically thin contrails cause a positive net forcing at top of the atmosphere. At the surface the radiative forcing is negative during daytime. The forcing increases with the optical depth and the amount of contrail cover. At the top of the atmosphere, a mean contrail cover of 0.1% with average optical depth of 0.2 to 0.5 causes about 0.01 to 0.03 Wm<sup>-2</sup> daily mean instantaneous radiative forcing. Contrails cool the surface during the day and heat the surface during the night, and hence reduce the daily temperature amplitude. The net effect depends strongly on the daily variation of contrail cloud cover. The indirect radiative forcing due to particle changes in natural cirrus clouds may be of the same magnitude as the direct one due to additional cover.

**Key words.** Atmospheric composition and structure (aerosols and particles) · Meteorology and atmospheric dynamics (climatology, radiative processes)

## 1 Introduction

Contrails are ice clouds with radiative effects similar to thin cirrus cloud layers (Liou, 1986; Raschke *et al.*, 1998). They are short-lived when formed in dry air but

persist and develop into extended cirrus cloud layers when the ambient air is moist with relative humidity above ice saturation. Individual contrails have been observed to persist for many hours (Minnis *et al.*, 1998). Satellite data reveal that persistent line-shaped contrail clouds cover at least 0.5% of central Europe at noon time in the annual average (Mannstein *et al.*, 1999). An analysis of meteorological data and aircraft fuel consumption data resulted in an estimate that such contrails cover about 0.1% of the globe with maximum cover values over the USA, Europe, the North Atlantic and the Indonesian area (Sausen *et al.*, 1998). The actual contrail cover is larger than suggested by line-shaped contrails in satellite pictures (Minnis *et al.*, 1998). Like thin layers of cirrus clouds, contrails are expected to enhance the ‘greenhouse effect’ because they reduce outward longwave (LW) flux more than they increase reflected shortwave (SW) fluxes (Platt, 1981; Stephens and Webster, 1981). However, measurements of downward fluxes below contrails from aircraft (Kuhn, 1970) and at the Earth’s surface (Sassen, 1997) revealed rather large reductions in downward SW flux in the shadow of individual contrails with little gain by infrared radiation leaving open the question of warming or cooling by contrails (Khvorostyanov and Sassen, 1998).

The radiative properties of cirrus clouds have been investigated in several studies (Ackerman *et al.*, 1988; Rockel *et al.*, 1991; Ebert and Curry, 1992; Fu and Liou, 1993). However, contrails differ from cirrus clouds in having relatively small vertical depth and occur mainly at temperatures below a threshold of order –40 °C (Schumann, 1996). Therefore, the ice water content (IWC) and ice water path (IWP) of contrails is smaller than for average cirrus clouds. On the other hand, contrails are formed from aircraft emissions which induce more and smaller ice particles in fresh contrail clouds (Kärcher *et al.*, 1996; Petzold *et al.*, 1997) so that the optical depth of contrails may be larger than that of cirrus with the same IWC. Aircraft emissions may also have indirect effects by modifying the microphysical

properties of cirrus clouds (Ström and Ohlsson, 1998b). The effect of aircraft aerosol in causing additional cirrus clouds, possibly long after emission, has not yet been determined.

Only a few studies have investigated the special radiative forcing properties of contrails (Grassl, 1990; Fortuin *et al.*, 1995; Strauss *et al.*, 1997). A systematic parametric study, covering the properties of contrails for various atmospheric conditions and seasons and for different traffic regions of the Earth, has not yet been reported. The indirect effect of changing particle sizes has been examined recently by Wyser and Ström (1998). In this study, we apply one-dimensional radiative transfer models for a sequence of relevant cases to determine the instantaneous or static radiative forcing (IPCC, 1996) for given cloud cover and fixed ambient conditions in the form of aircraft induced cirrus clouds. The next section reviews the available knowledge that guides this study. The methods used, the cases considered, and the results obtained in this study are presented and discussed thereafter, including a discussion of the indirect effect of aircraft by changing particle properties in cirrus clouds.

## 2 Radiative properties of contrails

The radiative properties of contrails depend on many parameters. Only a few recent studies have provided data suitable for modeling contrail radiative effects. Contrails are radiatively important only if formed in ice-supersaturated air, where they may persist and spread to several kilometers lateral width and a few hundred meters vertical depth (Detwiler and Pratt, 1984; Schumann and Wendling, 1990; Freudenthaler *et al.*, 1995, 1996; Sassen, 1997; Jäger *et al.*, 1998). In the solar range (near a wavelength of  $0.55\ \mu\text{m}$ ), the optical depth of observed persistent contrails varies typically between 0.1 and 0.5 (Kästner *et al.*, 1993; Jäger *et al.*, 1998; Minnis *et al.*, 1998; Sassen, 1997). Occasionally, very thick contrails (order 700 m) with optical depth greater than 1.0 are found at higher temperatures (up to  $-30\ ^\circ\text{C}$ ) (Schumann and Wendling, 1990; Gayet *et al.*, 1996). Contrail particles in young persistent contrails are typically smaller (mean radius of 5 to  $15\ \mu\text{m}$ ) than in other cirrus cloud types (greater than about  $30\ \mu\text{m}$ ) (Betancor-Gothe and Grassl, 1993; Brogniez *et al.*, 1995; Gayet *et al.*, 1996; Schröder *et al.*, 1998). The number density of ice crystals in contrails (order 10 to  $200\ \text{cm}^{-3}$ ) is much larger than in cirrus clouds (Sassen, 1997; Schröder *et al.*, 1998). The few measured values of the IWC in aged contrails vary between 0.7 and  $18\ \text{mg m}^{-3}$  (Gayet *et al.*, 1996; Sassen, 1997; Schröder *et al.*, 1998), consistent with numerical studies (Gierens, 1996; Khvorostyanov and Sassen, 1998).

The shape of contrail particles is important because clouds with aspherical particles may have smaller asymmetry factors causing a stronger solar albedo (Wendling *et al.*, 1979; Kinne and Liou, 1989; Liou *et al.*, 1998; Raschke *et al.*, 1998). Strong depolarization of Lidar returns by contrails with growing particles that

are a few minutes old indicate aspherical particles (Freudenthaler *et al.*, 1996; Sassen, 1997). Both, complex ice particles (Goodman *et al.*, 1998; Lawson *et al.*, 1998) and nearly spherical ice particles at low ambient temperatures ( $< -55\ ^\circ\text{C}$ ) using replicators in contrail cirrus (Schröder *et al.*, 1998) were identified. It seems that the amount of water vapor available in the core of contrails is too small, in particular at low temperatures, to let very many ice particles grow. Hence the particles in the core remain close to spherical while the particles near the humid boundary of contrails may become large and very complex in shape in particular at high ambient temperature and humidity (Heysfield *et al.*, 1998a). The large influence of particle shape on the scattering phase function was demonstrated in measurements (Gayet *et al.*, 1998) and computations (Liou *et al.*, 1998; Raschke *et al.*, 1998; Lawson *et al.*, 1998).

Contrail particles have been found to contain soot (Kuhn *et al.*, 1998; Petzold *et al.*, 1998; Ström and Ohlsson, 1998a, b). Soot in or on the ice particles may increase absorption of solar radiation by the ice particles and hence reduce the albedo of the contrails. The importance of the soot depends on the type of internal or external mixing and the volume fraction of soot enclosures (e.g., Chylek and Hallett, 1992). Since soot particles are typically less than  $1\ \mu\text{m}$  in diameter, their impact on the optical properties of the ice particles in aged contrails is likely small.

The day/night contrail cover ratio is of importance for the mean forcing because SW cooling is restricted to the daytime period while the LW heating acts all day. Diurnal coverage ratios of about 2 (Bakan *et al.*, 1994) over Europe and the eastern part of the North Atlantic, or 3 (Mannstein *et al.*, 1998) over central Europe have been deduced from satellite data consistent with a global mean noon/midnight traffic ratio of 2.8 (Schmitt and Brunner, 1997).

The change in radiative fluxes due to contrails has been computed with one-dimensional (1-D) models (Fortuin *et al.*, 1995; Strauss *et al.*, 1997). These studies treat contrails as a plane-parallel cloud in a homogeneously layered atmosphere and use area-weighted sums for fractional contrail cover. As a consequence, the contrail forcing grows linearly with contrail cover in these models. Inhomogeneity effects may be large in natural cirrus (Raschke *et al.*, 1998), but were considered small for vertically thin cloud layers in the few studies addressing this issue (Fouquart *et al.*, 1990; Schulz, 1998). Fortuin *et al.* (1995) computed the radiative forcing by contrails for fixed atmospheric temperatures for the North Atlantic flight corridor. Normalized to 100% contrail cover, a net forcing in the range of  $-30$  to  $+60\ \text{W m}^{-2}$  is found in summer and  $10$  to  $60\ \text{W m}^{-2}$  in winter. They used a highly parametrized radiative transfer model for cirrus with IWP values in the range of  $4$  to  $50\ \text{g m}^{-2}$  and crystal radius of  $4$  to  $100\ \mu\text{m}$ , implying optical depth values of  $0.05$  to  $20$ . They found a strong dependence on particle radius but do not discuss the accuracy of the model. The negative forcing values are computed for large IWP and small radius values. Wyser and Ström (1998) used a similar

model and discuss the particle impact in detail. Strauss *et al.* (1997) used a radiative convective model to simulate the climatic conditions of a mid-European region. They consider contrails and natural cirrus clouds with measured size spectra, but the particle size difference between the two cloud types considered is small (less than 20% in effective radius) so that the net radiative forcing for the two cloud types differs only a little. They find about  $30 \text{ Wm}^{-2}$  radiative flux change at the tropopause for 100% contrail cover with optical depth of 0.28 at  $0.55 \mu\text{m}$ ; and a surface temperature increase on the order 0.05 K for a 0.5% increase in current contrail cloud cover. With a 2-D radiative convective model, a 1 K increase was found in surface temperature over most of the Northern Hemisphere for an additional cirrus cover of 5% (Liou *et al.*, 1990). Using a global circulation model, the potential effects of contrails on global climate were simulated by introducing additional cirrus cover with the same optical properties as natural cirrus in air traffic regions with large fuel consumption (Ponater *et al.*, 1996). The induced temperature change was significant for 5% additional cirrus cloud cover in the main traffic regions. These studies demonstrate the importance of contrails in climate change and highlight the need for better understanding of the sensitivity of their radiative properties to all relevant parameters.

### 3 Methods and parameters

#### 3.1 Methods

In this section we present results of computations with 1-D radiative transfer models. The study uses three models, which we denote M, FL, and N, to quantify the sensitivity of the results to various established radiative techniques.

The model M is based on the matrix-operator-method (MOM) developed by Plass *et al.* (1973). The solar and terrestrial versions of this code performed successfully in an intercomparison of radiation codes (Ellingson and Fouquart, 1990). Fischer and Grassl (1984) described the shortwave version. The longwave version has successfully been applied in a comparison of modeled and measured broadband fluxes from aircraft data (Saunders *et al.*, 1992). In the solar spectral range, the radiative transfer code accounts for multiple scattering and absorption processes related to air molecules, aerosol/cloud particles, the absorbing gases, and the surface, in the longwave range additionally for the thermal emission of the relevant constituents. The solar spectral range, from  $0.2\text{--}4 \mu\text{m}$ , is divided into 25 wavelength intervals, the terrestrial spectral range from  $4\text{--}100 \mu\text{m}$  into 28 intervals. Average transmission functions accounting for gaseous absorption in the wavelength intervals are approximated by exponential sum fitting. The transmission functions result from line-by-line calculations based on the HITRAN-86 data base (Rothman *et al.*, 1987). The spectral extraterrestrial sun in the solar range is extracted from data incorporated in

the LOWTRAN-7 radiative transfer code (Kneizys *et al.*, 1988). The spectral optical parameters of ice clouds and aerosol particles are represented in each wavelength interval by the phase function (solar range), the asymmetry factor (terrestrial range), the volume extinction coefficient, and the single scattering albedo. For spherical particles, the spectral optical parameters are computed using Mie-theory on the basis of given particle size distributions and spectral complex refractive indices. In case of cirrus clouds/contrails, the refractive indices for ice according to Warren (1984) have been used, the refractive indices of the different aerosol components (Sect. 3.2) stem from WMO (1986). The properties of hexagonally shaped particles are taken into account only for the solar region and computed assuming geometrical optics (Hess and Wiegner, 1994). Strauss *et al.* (1997) describe the procedure and its application for contrails with the same size spectrum as used here (and for a cirrus with slightly different size spectrum). The calculations have been performed by the first author.

The model FL uses the radiative transfer code of Fu and Liou (1993) in the delta-4-stream model version (Liou *et al.*, 1998), including scattering and gaseous absorption of both LW and SW radiation. Although the model is highly resolved for absorption and scattering by gases and aerosols in both SW (54 bands) and LW (67 bands) spectra, it uses only 6 SW bands and 12 LW bands to compute particulate scattering and absorption and surface emissivities and albedos. The model has also been tested during the intercomparison of radiation codes (Ellingson and Fouquart, 1990) and applied for cloud studies (Charlock *et al.*, 1995). It uses spherical particles for liquid water at all wavelengths. For ice particles in the LW spectrum, the optical properties are computed using geometrical optics for hexagonal ice columns for size parameters less than 30 and a spheroidal approximation for smaller size parameters. In the SW regime, it uses optical properties resulting from randomly oriented columnar hexagon ray-tracing calculations for all particles. The calculations have been performed by the third author.

The model N is a radiative transfer code (Nakajima and Tanaka, 1986, 1988) including scattering and gaseous absorption using the delta-4-stream approximation, 400 bands in the shortwave range and 8000 bands in the longwave range with spectral data as in Kneizys *et al.* (1988). The model treats spherical particles or hexagonal particles as in Fu and Liou (1993). The calculations have been performed by the sixth author.

The methods are used to compute the sum of upward and downward fluxes in the SW and LW spectral range and the net fluxes (sum of SW and LW fluxes) at the TOA (actually 50 km), above the contrail layer, and at the surface (0 km altitude). The static radiative forcing is the difference in the fluxes at a certain level with and without inclusion of the contrail layer for otherwise constant conditions. A positive forcing at a certain altitude implies an energy gain of the system below that level. The results of these computations scale linearly with cloud cover.

### 3.2 Parameter values

The set of parameters necessary to assess the radiative impact of contrails consists of the vertical temperature, humidity, and aerosol profiles, surface temperature and its diurnal cycle, the altitude and geometrical thickness of the contrails, cloud cover, IWC, size spectra and the shape of the particles, surface scattering properties, latitude and the time of year determining solar zenith angle (SZA), and the daily variation of the contrail cover.

The parameters are specified according to the cases listed in Table 1. They cover the regions of most intense air traffic. The midlatitude continental summer, (a) is used as the reference case in the following. Case (d) is defined to approximate the Indonesian Equatorial region where a local maximum of contrail cover is expected (Sausen *et al.*, 1998). The latitude 62°N of the subarctic cases (e) and (f) covers the northern edge of the main traffic routes. It lies just south of the polar circle.

The surface properties in the solar range are approximated by Lambertian surface reflection with spectrally constant albedo. In the infrared range the surfaces are assumed to emit as black bodies in each wavelength interval. For the continental surfaces of cases (a) and (b), the surface albedo is taken as 0.2 (0.7 with snow cover). For the maritime cases (c), (d), (e), and (f), a value of 0.05 is chosen to represent a typical ocean albedo (except for the subarctic winter case with an ice albedo of 0.7).

The temperature and humidity profiles are specified for the selected regions and seasons as in the corresponding standard atmospheres of McClatchey *et al.* (1972). The surface temperature is kept temporally constant and equals the atmospheric temperature at the surface unless specified differently. The midlatitude continental summer atmosphere specifies 77% relative humidity at the surface, decreasing to 11% at the tropopause (12 km).

For model M, the aerosol properties are specified following WMO (1986). To calculate spectral phase functions and spectral optical parameters appropriate for the air mass of the midlatitude continental summer and winter atmospheres, the microphysical properties of the aerosol components connected to the profile ‘CONT-I’ of Table 2.3 in (WMO, 1986) are used. The profile is a composition of the aerosol types continental (0–12 km) and 75% H<sub>2</sub>SO<sub>4</sub> above 12 km. For the North Atlantic, tropical ocean, and subarctic summer and winter cases, the aerosol properties are calculated using the aerosol profile ‘MAR-I’ of WMO (1986), with

maritime aerosol (0–2 km), continental (2–12 km), and 75% H<sub>2</sub>SO<sub>4</sub> above 12 km. The 0.55-μm optical depth of the maritime aerosol (surface to 50 km) is 0.08, that of the continental aerosol is 0.28. In model FL, aerosols are specified with the same total column optical depth as for model M but using a Spinhirne (1991) distribution based on humidity. Scattering properties are based on either maritime or continental aerosols. Model N is applied without aerosols.

The model results depend critically on the assumed ice water content values. Up to now, no systematic study of IWC values in contrails is available. As observed for cirrus clouds (Heymsfield and Platt, 1984), the IWC of contrails may depend on ambient temperature because the amount of water available between liquid and ice saturation increases with temperature for temperature less than −12 °C (Ludlam, 1980). Contrails with small particles have little chance for precipitation and, hence, may contain more ice than aged cirrus clouds. For modeling, we assume that the IWC is determined by a fraction (1/2) of the amount of water available for ice formation between the limit of ice nucleation and ice saturation. Heymsfield *et al.* (1998b) find that the limit for ice nucleation decreases almost linearly with respect to relative humidity (RH) from water saturation (100% RH) at temperatures above −39 °C to 75% RH at and below −55 °C. In principal, the IWC will depend on many other atmospheric parameters and may exceed the limit of potential IWC at a given level when contrails form in rising air.

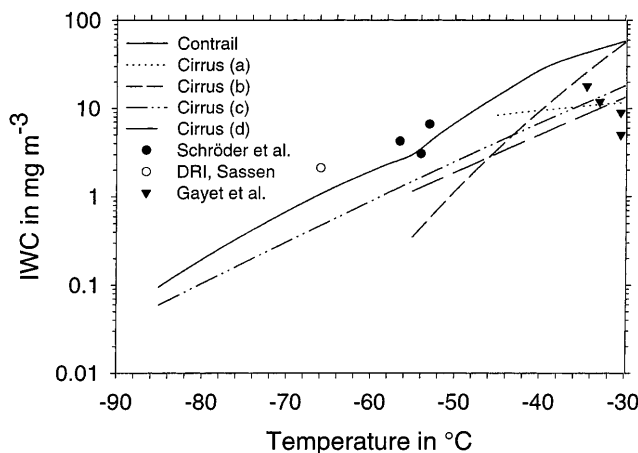
Figure 1 compares the IWC of the model contrail as a function of temperature with the IWC in cirrus clouds as obtained from measurements over Wisconsin (a), various places in the USA (b), and in a tropical cirrus (c), using interpolations as given in Heymsfield (1993). Curve (d) (Stephens *et al.*, 1990; correction in Sinha and Shine, 1994) fits earlier data from midlatitude cirrus over the USA (Heymsfield and Platt, 1984). Individual IWC values measured in cirrus clouds may deviate from the curves by more than a factor of ten. We see that the model gives IWC values which are slightly greater than the values measured in natural cirrus clouds. Figure 1 also shows the few data points which are available from direct measurements in aged contrails (Gayet *et al.*, 1996; Sassen, 1997; Schröder *et al.*, 1998). While the data of Sassen and Schröder support the IWC model within reasonable limits, Gayet *et al.* (1996) find IWC values at various altitudes in a single contrail that are smaller and decrease with temperature. Deviations between the measured IWC values and any systematic trend are not surprising because of the difficulties in

**Table 1.** Cases (a) to (f)

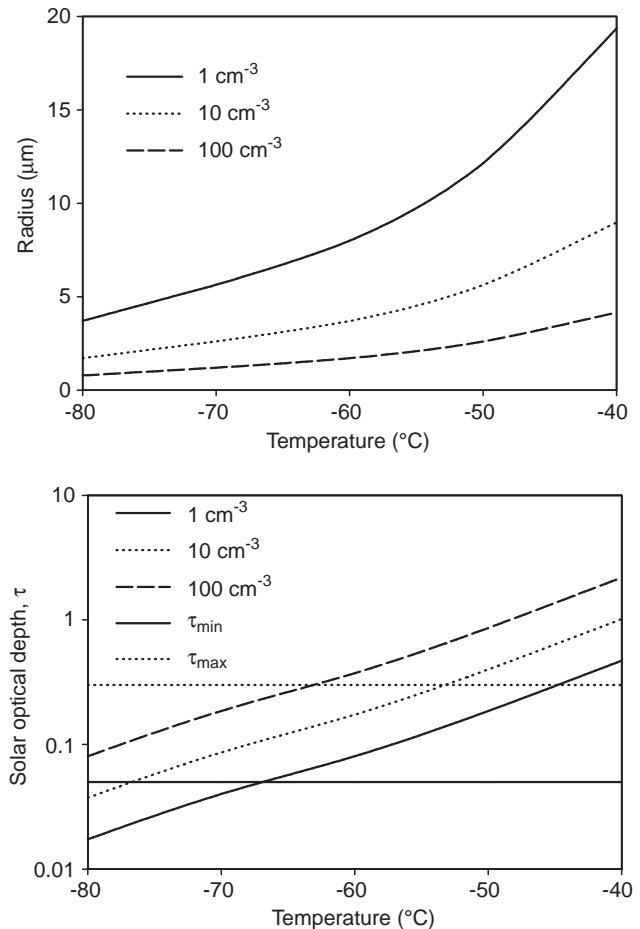
Case	Region	Date	Latitude in °N	Minimum SZA in°	Daytime fraction
a	Midlatitude continent	21 June	45	21.7	0.64
b	Midlatitude continent	21 December	45	68.4	0.35
c	North Atlantic ocean	21 June	55	31.6	0.71
d	Tropical ocean	21 June	0	23.5	0.5
e	Subarctic ocean	21 June	62	38.6	0.19
f	Subarctic ocean	21 December	62	85.5	0.79

measuring IWC inside a contrail, which are due to the shortcomings of the various sensors and the representativity of such measurements in a contrail cloud which is highly heterogeneous spatially. Figure 2a shows the volume mean radius of ice particles as it would result for monodisperse ice particles of typical ice particle concentrations in contrails and the modeled IWC. Figure 2b shows the optical depth  $\tau$  which a cloud of 200 m geometrical thickness which is composed of these particles would have for an optical extinction efficiency of 2. As can be seen, the range of computed values is consistent with data from measurements as cited in Sect. 2 and indicates that the IWC estimate is reasonable. As expected, the computed particle sizes vary by a factor  $100^{1/3} = 4.6$  for a factor 100 variation in particle concentration, and are within the range of particle sizes reported. The computed optical depth matches the range of 0.05 to 0.3 measured by Jäger *et al.* (1998). It would match even better if the particle concentration decreased with temperature, which may well be the case due to reduced nucleation rates at higher ambient temperatures (Kärcher *et al.*, 1996). Unfortunately, the temperature dependence of contrail particle radius, concentration, and optical depth values has not been documented. Obviously, many more measurements are needed for reliable estimates of IWC in contrails.

Table 2 characterizes the various cases in terms of contrail layer altitudes and relevant temperatures. The contrail is represented as a temporally constant cloud cover of thin cirrus of 200 m vertical depth between 10.8 and 11 km altitude (except for the subarctic atmospheres with contrails located between 8.8 to 9 km) with a realistic particle size spectrum as given by Strauss *et al.* (1997) (volume-mean particle diameter = 16.4  $\mu\text{m}$ ). In the reference case, the IWC is 21  $\text{mg m}^{-3}$ , the ice water



**Fig. 1.** Ice water content (IWC) versus ambient temperature. The solid curve is the proposed contrail IWC model of this study. The various dashed curves represent fits to IWC values observed in cirrus over (a) Wisconsin, (b) various parts of continental USA, (c) tropical cirrus (Heymsfield, 1993) and a fit (d) (Stephens *et al.*, 1990; Sinha and Slingo, 1994) for midlatitude cirrus data of Heymsfield and Platt (1984). The symbols denote individual IWC data measured in aged contrail cirrus by Gayet *et al.* (1996), by the Desert Research Institute (see Sassen, 1997), and Schröder *et al.* (1998)



**Fig. 2a, b.** Particle radius and solar optical depth  $\tau$  versus temperature for a 200 m thick contrail for three values of particle number concentration of monodisperse particles. IWC as given by the solid curve of Fig. 1, and extinction efficiency of 2. The two horizontal lines in the lower panel denote the range of data ( $\tau = 0.05$  to 0.3) obtained by Jäger *et al.* (1998)

path is  $\text{IWP} = 4.4 \text{ g m}^{-2}$ , and the optical depth is  $\tau = 0.52$ .

The reference case assumes spherical ice particles mainly for simplicity but also because contrail particles have been found to be about spherical when collected on impactors at least in young contrails and at low ambient temperatures (Schröder *et al.*, 1998). On the other hand, observations (see Sect. 2), indicate that contrail particles deviate from spherical shape after some time in aging contrails in particular at high ambient temperatures. Therefore, calculations are also performed with clouds of hexagonal particles of the same IWC.

## 4 Results

The shortwave (SW), longwave (LW), and net radiative flux changes are listed in Table 3 for reference case a), see Tables 1 and 2, as computed with model M for spherical and model FL for hexagonal ice particles at three levels of the atmosphere. Table 3 shows daily means of the instantaneous values that are computed as

**Table 2.** Contrail and tropopause altitude and temperature values for cases (a) to (f)

Region	Contrail top altitude in km	Contrail top temperature in °C	Surface temperature in °C	Tropopause altitude in km	Tropopause temperature in °C
a Midlatitude summer continent	11	−44.2	20.8	12	−51.2
b Midlatitude winter continent	11	−54.0	−1.0	10	−54.2
c North Atlantic summer ocean	11	−44.2	20.8	12	−51.2
d Tropical ocean, June	11	−43.2	26.8	17	−78.2
e Subarctic summer ocean	9	−41.2	13.8	10	−48.0
f Subarctic winter ocean	9	−56.0	−16.1	9	−56.0

averages over 24 hours including the diurnal variation of the solar zenith angle on 21 June at 45°N for 100% cloud cover. Also listed is the daytime mean of the net forcing. The daytime mean is the average over the period from sunrise to sunset (see Table 1 for daytime fraction), whereas the daily mean is the average over the 24 hours of a day. The daytime mean SW forcing equals the daily mean divided by the daytime fraction. The nighttime mean equals the LW forcing, which is constant throughout the day because of assumed constant temperatures.

In the reference case, a constant 100% contrail cover with spherical particles causes a positive static radiative forcing in the daily average of about  $40 \text{ Wm}^{-2}$ . The TOT (top of troposphere) value is slightly larger, indicating a slight cooling of the stratosphere. The TOA and TOT flux changes due to contrails differ by only about 10%. When adjusting the stratospheric temperature to the change in net radiative forcing, the TOA and TOT forcing values are expected to become equal and equal to a value in between the static TOA and TOT values. Hence, the static TOA flux change gives a reasonable approximation for the adjusted radiative forcing considered in IPCC (1996). At the surface, the LW flux changes are much smaller because of strong absorption by water vapour, while the SW flux changes are only a little smaller than at TOA because the atmosphere is largely transparent to solar radiation. The net flux change is negative at the surface, as observed by Sassen (1997), but smaller in magnitude than at TOA. The day time SW contribution dominates and cools the surface also in the daily mean. During daylight only, the net forcing is about 20 to 30% smaller, but still positive for TOA. At the surface, the daytime mean net forcing is negative and more than a

factor of 2 larger than the daily mean. Hence, the surface forcing depends strongly on the daily cycle of contrail cover.

The results of the parametric study for various regions, seasons and particle shapes are shown in Table 4, as computed with models M and D. The contrails cause negative SW and positive LW flux changes. For reasons to be discussed in Sect. 5, the magnitude of the SW forcing is larger over dark ocean areas than over bright snow surfaces, while the LW forcing is larger in the tropics than in polar regions. The net forcing over the midlatitude continent is larger in summer than in winter. In all cases considered the net forcing is positive, suggesting that contrail heating of the atmosphere prevails over cooling. Hexagonal particles cause a more negative SW forcing and less net forcing, therefore.

The net fluxes depend strongly on the assumed IWP or optical depth. Figure 3 shows the computed SW, LW and net change in radiative fluxes at TOA and at the surface for 100% contrail cloud cover for the reference case with spherical particles as computed with model M. The IWC was varied to yield different values of the optical depth  $\tau$  at  $0.55 \mu\text{m}$ . At TOA, the LW forcing is larger than the SW. The net radiative forcing grows linearly with  $\tau$  for small values of  $\tau$  but soon approaches a maximum of about  $60 \text{ Wm}^{-2}$  near  $\tau = 3$  (IWP of about  $25 \text{ g m}^{-2}$ ). The exact value of this maximum depends on details of the particle properties, cloud location, temperature, surface properties, and time of year. For larger values of  $\tau$  the net forcing decreases and becomes negative in our case for  $\tau > 10$  (IWP  $> 80 \text{ g m}^{-2}$ ), but contrails are probably never that thick. Our results are qualitatively very similar to those for cirrus clouds presented by Rockel *et al.* (1991), Fu and Liou (1993), Jensen *et al.* (1994), Fortuin *et al.* (1995), and Strauss *et al.* (1997), who report maximum net forcing values of 30 to  $80 \text{ Wm}^{-2}$  at comparable IWP or optical depth values. The quantitative differences are likely the result of different case specifications. Based on this analysis, contrails are expected to heat the atmosphere below them.

In the diurnal cycle, radiative forcing by contrails at TOA is positive and strongest during night. For small optical depth, the net forcing at TOA is also positive during day and, hence, always positive regardless of the diurnal cycle of contrail cover. As can be seen from Table 5 and Fig. 4, for an optical depth of 0.52, the negative SW forcing at TOA is maximum not at noon

**Table 3.** Daily mean (24 h) and daytime mean (from sunrise to sunset) radiative flux changes in the midlatitude summer continental case at top of the atmosphere (TOA, 50 km), top of troposphere (TOT, 12 km), and at the surface (SUR, 0 km) in  $\text{Wm}^{-2}$ . Results from model M for spherical particles

Altitude	Daily mean			Daytime mean		
	SW	LW	Net	SW	LW	Net
TOA	−13.4	51.6	38.2	−21.0	51.6	30.6
TOT	−13.8	55.6	41.8	−21.5	55.6	33.1
SUR	−12.7	7.4	−5.3	−20.0	7.4	−12.6

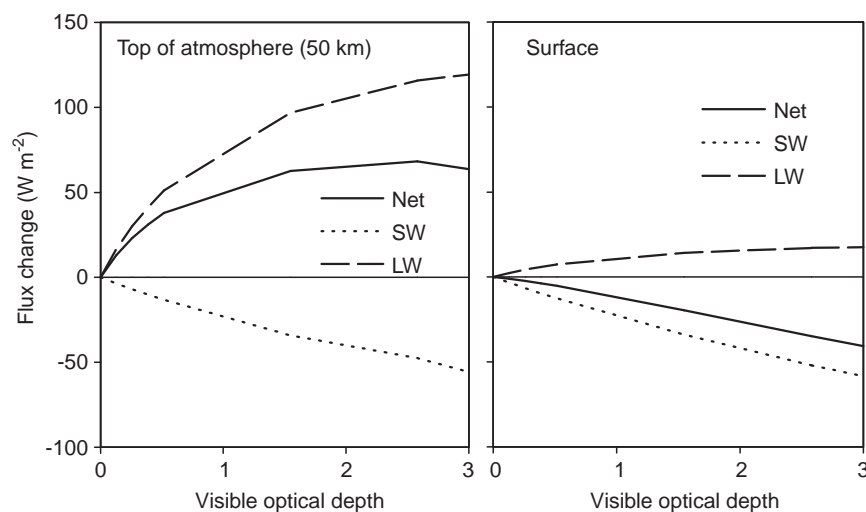
**Table 4.** Daily mean TOA radiative flux changes for shortwave (SW), longwave (LW), and Net(=SW + LW) radiation for 100% contrail cover in various regions and seasons, with prescribed surface albedo, with contrail ice water content IWC, and computed

Region	Surface albedo	IWC in $\text{mg m}^{-3}$	$\tau$	SW $\text{Wm}^{-2}$	LW $\text{Wm}^{-2}$	Net $\text{Wm}^{-2}$
Midlatitude summer continent, 45°N	0.2	21	0.52	−13.4 −22.0	51.6 51.5	38.2 29.5
Midlatitude winter continent, 45°N	0.2	7.2	0.18	−4.2 −4.6	18.4 18.3	14.2 13.7
Midlatitude winter continent with snow, 45°N	0.7	7.2	0.18	−2.3	18.4	16.1
North Atlantic summer ocean, 55°N	0.05	21	0.52	−2.0 −21.5 −32.7	18.3 53.3 50.9	16.3 31.8 18.2
Tropical ocean (Equator., June)	0.05	23	0.57	−16.0 −25.9	63.0 57.4	47.0 31.5
Subarctic summer ocean, 62°N	0.05	28.2	0.70	−30.8 −45.3	55.7 49.1	24.9 3.7
Subarctic winter ocean ice 62°N	0.7	7.2	0.18	−0.6 −0.7	14.6 13.2	14.0 12.5

**Table 5.** Variation of the shortwave (SW), longwave (LW) and net radiative flux change in  $\text{Wm}^{-2}$  as a function of solar zenith angle (SZA) and morning hours, results of model M for spherical

particles, for the reference case (midlatitude summer continent), at TOA and at the surface. The value SZA = 21.7° is the minimum value on 21 June at 45°N

Altitude	SZA in° Time of day	21.7 12.00	30 10.29	40 9.23	50 8.26	60 7.31	70 6.36	80 5.35	90 <4.29
50 km	SW	−12.1	−14.4	−16.7	−21.7	−28.7	−33.6	−28.1	0
	LW	51.6	51.6	51.6	51.6	51.6	51.6	51.6	51.6
	Net	39.4	37.1	34.8	29.9	22.8	17.9	23.4	51.6
Surface	SW	−17.8	−18.7	−23.3	−27.3	−27.7	−22.9	−12.9	0
	LW	7.4	7.4	7.4	7.4	7.4	7.4	7.4	7.4
	Net	−10.4	−11.3	−15.9	−19.9	−20.3	−15.5	−5.5	7.4



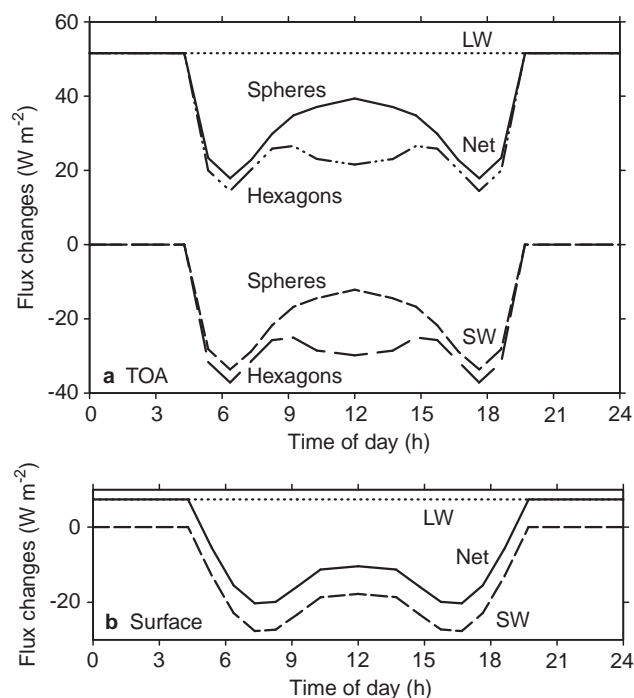
**Fig. 3.** Daily mean instantaneous shortwave (SW), longwave (LW), and net forcing versus 0.55  $\mu\text{m}$  optical depth at 50 km altitude (TOA) and at the surface for 100% contrail cover with spherical ice particles for the midlatitude summer continent reference case (a)

but during morning or afternoon hours when the solar zenith angle is near 60 to 70°. The difference between spherical and hexagonal particles is largest around noon at smallest SZA. Kinne and Liou (1989) find similar results for thin cirrus clouds. They find that the net forcing may become even negative near solar zenith angles of 50 to 80° in case of cirrus clouds of large

hexagonal ice crystals. We, too, find smaller, but still positive values (possibly because of a different particle size spectrum) of the net forcing at TOA for large zenith angles when using hexagonal particles (model M), see Fig. 4a.

Other than at TOA, the net flux change is negative at the surface even for thin contrails during the day,





**Fig. 4a, b.** Flux changes **a** at top of atmosphere (TOA) and **b** at the surface versus time of day for shortwave (SW), longwave (LW), and net (SW + LW) fluxes for spherical and hexagonal (shown for TOA only) particles in a contrail with optical depth of 0.52, case (a)

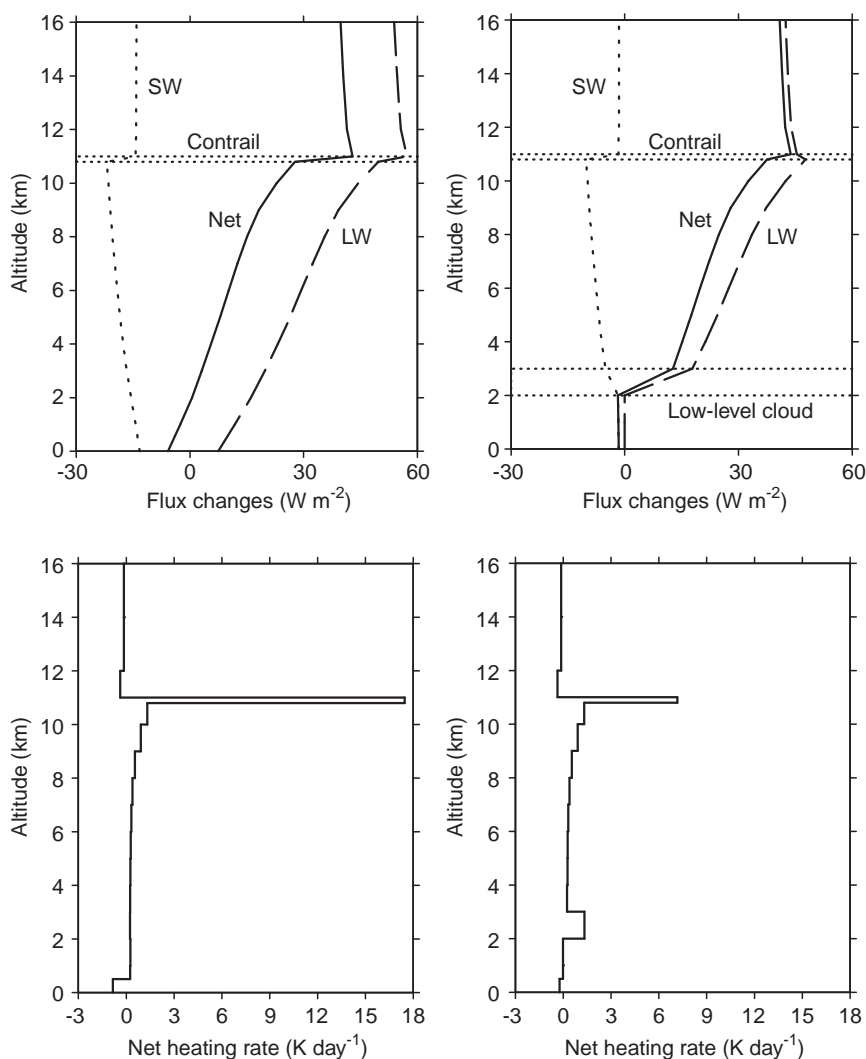
causing maximum cooling at solar zenith angles near  $50^\circ$  to  $60^\circ$  (see Table 5 and Fig. 4b). The maximum SW cooling is approximately 20 to 25  $\text{W m}^{-2}$ , while the maximum LW warming is about 5 to 10  $\text{W m}^{-2}$  (see Table 2). Similar values were computed recently by Khvorostyanov and Sassen (1998). Hence, the maximum day-night difference in net radiative forcing at the surface for otherwise cloudless summer mid-latitude conditions amounts to about 20  $\text{W m}^{-2}$  for constant 100% contrail cover with optical depth of 0.5 and constant surface temperature. The daily forcing amplitude due to contrails will be smaller when accounting for the change in LW forcing due to the daily surface temperature cycle. Also increased low-level humidity and low-level cloud cover reduce this forcing amplitude.

As shown in Fig. 5, contrails change the profiles of radiative fluxes and volumetric heat sources within the atmosphere and the energy budget at the surface. The perturbed surface energy budget induces surface temperature changes depending on the heat flux into the ground, evaporation, and the depth of the atmospheric boundary layer that exchanges heat with the surface. For an adiabatic surface with uniform distribution of the contrail induced heat source over the lowest, say, 500 m of the atmosphere, a change in net heat budget at the surface by  $-5.3 \text{ W m}^{-2}$  in the daily mean (see Table 3) would cool that layer at a rate of  $0.8 \text{ K day}^{-1}$ . Similarly, a day-night difference of  $-20 \text{ W m}^{-2}$  over 12 hours would reduce the daily temperature range by 1.4 K if the radiation heat gets distributed over the lowest 500 m atmosphere only (0.7 K for 1000 m). A constant 100% contrail cover lasting the whole day is, of course, unlikely.

Above the surface, Fig. 5 shows the contrail induced volumetric heat source given by the change in divergence of the sum of the solar and infrared radiation fluxes (Loiu, 1986, Ackerman *et al.*, 1988). In the reference case, the 200 m deep contrail layer gets heated at a rate of 17 K/day for 100% contrail cover at about equal fractions by LW and SW flux changes, while the stratosphere above the contrail gets cooled and the troposphere below the contrail layer gets heated mainly in the LW range at a rate of order 0.3 K/day. A contrail above a thick lower-level cloud heats the atmosphere mainly above the lower cloud; the heating rates are much smaller below the cloud. This is illustrated in Fig. 5 for a low-level cloud with water droplets of  $5 \mu\text{m}$  mode radius, a lognormal size distribution, and a concentration of  $100 \text{ cm}^{-3}$  at 2 to 3 km altitude with an optical depth of 23 at  $0.55 \mu\text{m}$ .

Finally, the sensitivity of contrail forcing to other important parameters is studied. The midlatitude continental summer atmosphere, case a) of Table 2, is considered as reference, but for fixed solar zenith angle of  $60^\circ$  and an assumed daytime fraction of 50%. Figure 6 shows the results of model N separately for SW, LW and net forcing at TOA. Aspherical particles cause stronger SW cooling because of larger side-ward scattering and less forward scattering. The net forcing results are sensitive to the solar zenith angle, optical depth of the contrails (ice water content), particle radius, presence of lower level clouds, surface albedo, and relative humidity profile. The SW forcing is much more negative at a solar zenith angle of  $60^\circ$  compared to  $21.7^\circ$ . The forcing increases with the optical depth (or the IWC). The increase is nearly linear for the SW part but less than linear for the LW part. For the same IWC, contrail with particles of  $5 \mu\text{m}$  mean radius cause more radiative forcing than contrails with larger particles. Variations in surface temperature (here by  $\pm 5 \text{ K}$ ) cause a relatively small net flux change but the heating effect of contrails is higher over a warmer surface. The net forcing is larger over a surface with higher surface albedo because of less negative SW forcing. Low-level clouds at 2 to 3 km altitude, as in Fig. 5, with large cover and optical depth of 23 at  $0.55 \mu\text{m}$  reduce both the SW and the LW forcing of the cloud-free case below a contrail, causing a small net increase of the forcing. A contrail above a low level cloud causes larger net heating because of a high albedo and relatively high temperature of the lower cloud. Thick clouds below contrails may also reduce net heating when high and cold. The LW forcing decreases when the humidity in the atmosphere below the contrail increases because of reduced upward LW flux reaching the contrail. The geometrical thickness of the contrails is unimportant as long as the IWP remains unchanged. Lowering the altitude of a contrail for fixed IWC reduces the LW effects slightly because of higher ambient temperature at the lower contrail level. However, adapting the IWC to the warmer atmosphere makes the lower contrail optically thicker and radiatively more effective than the higher contrail.

Hence, contrails heat most when covering a warm and bright surface. Contrail heating increases with IWP



**Fig. 5.** Vertical profiles of shortwave (SW), longwave (LW) and net flux changes (*top*) and net heating rate (*bottom*) induced by a contrail (at altitude as indicated by *horizontal dotted lines*) for the reference case (*left*, optical depth 0.52; case a) and the same case but with a low-level water cloud at 2–3 km altitude (*right*). The net heating rate is plotted as mean values over certain altitude intervals as indicated by the step functions. The flux profile is the linear interpolation between the flux values at the boundaries of these altitude intervals. The heating rate near the surface illustrates the net change in the radiative heat budget at the surface assuming adiabatic surfaces and a uniform mixing of heat across the lowest 500 m of the atmosphere

for small IWP values. As a whole, the TOA radiative forcing is only weakly sensitive to key parameters except for the optical depth and the contrail cover, with which the forcing scales about linearly. Representative net forcing values are 20 to 50  $\text{W m}^{-2}$  for 100% contrail cover and optical depth of 0.5 at  $0.55 \mu\text{m}$ .

## 5 Discussion

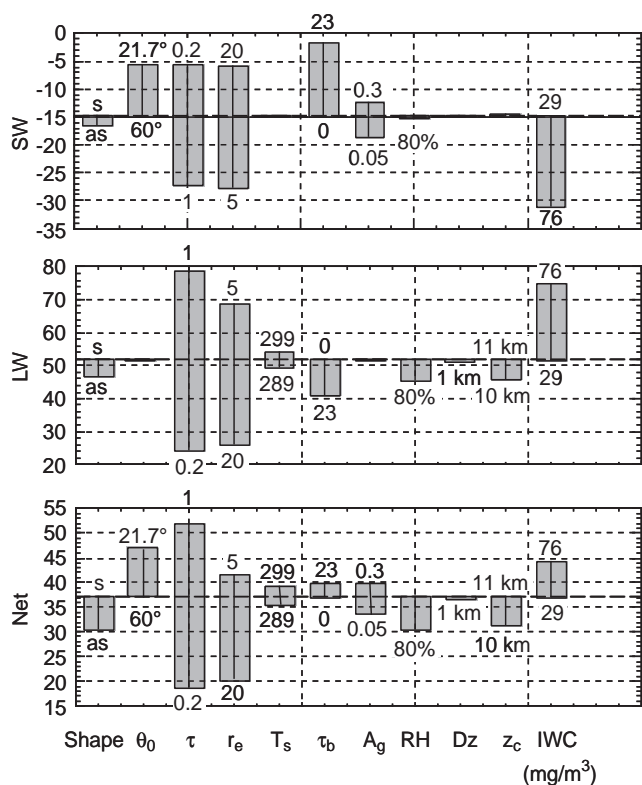
### 5.1 Model differences

Table 6 lists the net forcing results for the parameter study shown in Fig. 6 as obtained from the three models FL, M, and N. The model results agree well with each other. The largest model differences are found for aspherical particles which are represented with different shapes in various spectral regions in the models, but all show stronger SW cooling and therefore smaller net forcing for aspherical particles than for spherical ones, as expected from Kinne and Liou (1989). Otherwise the differences between the results from the three models, with various flux approximations and spectral resolutions, differ by less than 7% from each other. This is

consistent with findings from other model comparisons for optically thin clouds (King and Harshvardhan, 1986). Similar to cirrus cases (Ackerman *et al.*, 1988), any errors in the scattering properties of individual particles is dwarfed by the uncertainty in the assumed IWP values of contrails. The tropospheric aerosol slightly enhances the planetary albedo and the absorption properties, reducing both the SW and LW contrail forcing. If mode M is applied for the reference case (a) using maritime aerosol (aerosol optical depth of 0.08 at  $0.55 \mu\text{m}$ ) instead of the continental aerosol (optical depth 0.28), the contrail forcing increases from 38.16 to 39.71  $\text{W m}^{-2}$  for 100% contrail cover. Obviously, the background aerosol properties are of minor importance, as shown also by the good agreement between models M and N, where N has been applied to the contrail cases for zero background aerosol.

### 5.2 Forcing by a layer of contrail cirrus

In all cases, the computations show positive values of the net forcing at TOA, suggesting that contrail heating generally prevails over cooling in the atmosphere/surface system. This can be understood as follows.



**Fig. 6.** Results of a sensitivity study using model N. The bars indicate the range of variation of shortwave (SW), longwave (LW) and net (Net) flux changes in  $\text{Wm}^{-2}$  for 100% contrail cover due to the given variation of the parameters: particle shape, solar zenith angle  $\theta_0$ , IWC or optical depth  $\tau$ , volume-mean particle radius  $r_e$  (in  $\mu\text{m}$ ), surface temperature  $T_s$  (K), optical depth of lower level cloud  $\tau_b$ , ground albedo  $A_g$ , ambient relative humidity  $RH$  (% of liquid saturation), contrail layer depth  $Dz$  (km), cloud top level  $z_c$  (km), and contrail at 1 km lower level but with increased ice water content  $IWC$  ( $\text{mg m}^{-3}$ )

The shortwave (SW) radiative forcing  $F_{SW}$  of contrails is

$$F_{SW} = -S\Delta A,$$

where  $S$  is the solar irradiance and  $\Delta A$  is the difference of the system albedo  $A$  with and without a contrail. The SW forcing is negative when the cloud increases the

albedo. This is the case in most instances. Exceptions occur over surfaces with very large surface albedo  $A_g$  and sufficient absorption in the atmosphere between contrail top and the surface. For 100% coverage, the change in albedo is

$$\Delta A = R(1 - A_g)^2 / (1 - RA_g),$$

where  $R$  is the reflectance of the cloud layer and  $A_g$  the effective ground albedo (Paltridge and Platt, 1976, p. 235). Hence, the SW forcing grows as  $(1 - A_g)^2$  for small cloud reflectance,  $R < 0.1$  (Charlson *et al.*, 1992). In the reference case, the forcing is close to linear in  $(1 - A_g)$ . In any case, SW forcing has a greater magnitude over dark surfaces than over bright surfaces. The reflectance  $R$  of a thin, non-absorbing cloud layer,

$$R = \beta\tau / \cos(\theta_0),$$

increases with the upward scattered fraction  $\beta$  of the incident light, the optical depth  $\tau$ , and the solar zenith angle  $\theta_0$ . The value of  $\beta$  depends on the scattering phase function of the ice particles and the solar zenith angle. In the two-stream approximation, the upward scattered fraction  $\beta$  of diffuse light increases with  $(1 - g)$ , where  $g$  is the asymmetry factor (Paltridge and Platt, 1976, p. 76). For directed radiation, backscatter increases approximately as

$$\beta = 1/2 - (3/4)(g/(1 + g))\cos(\theta_0)$$

(see Rockel *et al.*, 1991). Hence, the shortwave forcing is larger for smaller  $g$ , and therefore larger for hexagonal ice particles than for spherical particles (Wendling *et al.*, 1979; Kinne and Liou, 1989; Rockel *et al.*, 1991). The optical depth can be estimated for monodisperse thin clouds from

$$\tau = 3 \text{ IWP} Q_e / (4 r \rho_{ice}),$$

with extinction efficiency  $Q_e$ , particle radius  $r$ , and ice density  $\rho_{ice}$ . For particle radius  $r$  large compared to the typical wavelength  $0.55 \mu\text{m}$  of the solar range, the extinction efficiency is close to a constant,  $Q_e = 2$ . Hence, for fixed IWP, clouds containing smaller particles have larger optical depth and larger solar albedo (Twomey, 1977).

**Table 6.** Sensitivity of the daily mean net TOA flux change by contrails to various parameters for 100% contrail with given optical depth  $\tau$  at  $0.55 \mu\text{m}$ . Results from models N, FL, and M, where available

Case/parameters	Parameter range	$\tau$	Net forcing in $\text{Wm}^{-2}$		
			N	FL	M
Reference		0.52	37.1	37.2	37.2
Different aspherical particles	Spherical – aspherical	0.4	37–22	37–34	37–36
Solar zenith angle	$60^\circ$ – $21^\circ$	0.52	37–48	37–45	37–46
Ice water content (IWC)	$7.2$ – $42 \text{ mg m}^{-3}$	$0.2$ – $1.0$	19–51	18–53	19–52
Particle radius	$5$ – $20 \mu\text{m}$	$0.85$ – $0.21$	41–20	–	–
Surface temperature	$289$ – $299 \text{ K}$	0.52	34–39	36–39	35–40
Optical depth of low-level clouds	$0$ – $23$	0.52	37–40	37–39	37–40
Surface albedo	$0.05$ – $0.3$	0.52	31–40	34–39	34–40
Relative humidity	Reference – 80%	0.52	37–31	37–31	37–31
Contrail depth (for fixed ice water path)	$200 \text{ m}$ – $1 \text{ km}$	0.52	37–37	–	37–37
Lower contrail top (for fixed IWC)	$11$ – $10 \text{ km}$	0.52	37–31	37–32	37–31
Lower contrail top (increased IWC)	$11$ – $10 \text{ km}$	$0.52$ – $1.32$	37–45	–	37–41

The LW forcing by a 100% cover of contrails, which is given approximately by

$$F_{\text{LW}} = \sigma \varepsilon (T_e^4 - T_b^4),$$

with Stefan-Boltzmann constant  $\sigma$ , is greatest when the difference between contrail temperature  $T_e$  and brightness temperature  $T_b$  of the atmosphere below the contrail is large (i.e., larger over warm than over cool surfaces, larger in a dry than in a humid atmosphere) and the contrail emissivity  $\varepsilon$  is large (Ebert and Curry, 1992, Fu and Liou, 1993). The brightness temperature  $T_b$  is smaller than the ground temperature  $T_g$ , in particular over humid atmospheres and low-emissivity surfaces. In the absorption approximation (Paltridge and Platt, 1976, p. 197), the contrail emissivity is

$$\varepsilon = 1 - \exp(-\beta_a \Delta z)$$

and, for monodisperse contrail cloud, the volume absorption coefficient

$$\beta_a \Delta z = 3 \text{ IWP } Q_a / (4 r \rho_{\text{ice}})$$

increases with the ice water path (IWP). The absorption efficiency  $Q_a$  increases in fairly linear manner with particle radius up to radius of order 10 to 20  $\mu\text{m}$  (Paltridge and Platt, 1976, p. 195) and thereafter approaches its asymptotic value of 1.0. Therefore, the emissivity of the contrail is fairly independent of particle radius for effective particle radius less than about 10  $\mu\text{m}$ , and decreases with particle radius for larger particles. For increasing IWP values, the emissivity approaches one and “saturates” (approaches a constant) quickly when the particles are small while the albedo is still much smaller than one (Stephens and Webster, 1981). Use of spheres instead of more realistic ice particle shapes may overestimate the absorption by ice particles but only to a minor degree in the infrared regime (Ackerman *et al.*, 1988; Fu *et al.*, 1998).

The water vapor that is converted to ice during contrail formation has an opposing radiative effect. The water-vapor-induced LW forcing increases strongly with altitude and depends on the temperature and water vapor profiles. In the tropical reference atmosphere, a 10% increase in humidity in a small vertical range at 11 km altitude causes a LW forcing of 0.4  $\text{W m}^{-2}$  ( $\text{g m}^{-2}$ )<sup>-1</sup> when normalized to the added water vapor mass column (Schmetz *et al.*, 1995). Thus the ice mass path of 4.6  $\text{g m}^{-2}$  contained in the tropical contrail causes 0.2  $\text{W m}^{-2}$  LW forcing as gas. The ice cloud causes 60  $\text{W m}^{-2}$  of LW forcing (see Table 4). Hence water in the ice phase is about 300 time more effective radiatively than water as vapor at the altitudes of contrails. Therefore, the reduction of water vapor concentration during contrail formation is of little radiative importance.

The net radiative forcing of clouds is the sum of the SW and LW flux changes and may be positive or negative. Thin contrails with small reflectivity but rather large emissivity cause a small but positive radiative forcing at TOA, while thick cirrus clouds may cause a cooling (Stephens and Webster, 1981; Fu and Liou,

1993). Maximum heating is reached at intermediate IWP of order 20  $\text{g m}^{-2}$ , corresponding to an optical depth of about 2 to 3, and the net forcing becomes negative for large IWP greater than an order 100  $\text{g m}^{-2}$  with optical depths greater than about 10 to 20 (Jensen *et al.*, 1994).

The calculations show that contrails cause a positive net forcing at TOA in most cases. Exceptions are possible for situations where contrails form over very cold surfaces with low albedo, at SZA near 60 to 70°, over a very humid but cloud free troposphere, and for contrails with very small particles (<10  $\mu\text{m}$ ), particles with small asymmetry factor (as for some ice crystals), and contrails with large optical depth (>10). In fact, Fortuin *et al.* (1995) find negative forcing only for large IWP values (>25  $\text{g m}^{-2}$ ) and small crystal radius (<8  $\mu\text{m}$ ), implying optical depth values larger 20, far larger than observed for contrails.

Based on the assumed IWP values, the computations suggest that the contrails have optical depth values in between 0.2 and 0.7 and cause net TOA forcing for 100% contrail cover between about 10  $\text{W m}^{-2}$  and 30  $\text{W m}^{-2}$  in the annual mean, and little more in tropical regions. If the global contrail cover is of order 0.1% as computed by Sausen *et al.* (1998), the global mean radiative forcing is of order 0.01 to 0.03  $\text{W m}^{-2}$ . Hence, the global radiative forcing by contrails is much smaller than that due to other anthropogenic changes in the last century (1.5  $\text{W m}^{-2}$  according to IPCC, 1996), but comparable to the 0.007 to 0.024  $\text{W m}^{-2}$  forcing by past emissions of carbon dioxide by aircraft (Brasseur *et al.*, 1998). If contrails occur only during the day and not during the night, the positive forcing by contrails at TOA would be smaller by about 20 to 30%, and the negative forcing at the surface would be 100% larger. Our results depend also strongly on the assumed IWC, the geometrical thickness of the contrails, and the particle sizes of the contrails, all together controlling the optical depth of the contrails. Contrails could have a factor of 3 smaller IWC than assumed in this study (see Fig. 1), may be geometrically thicker by a factor of 3 (Freudenthaler *et al.*, 1996; Sassen, 1997), and the particle size is known, at best, to a factor of 2, implying an uncertainty in optical depth of about factor 4 (based on the square of the sum of the individual uncertainty factors). The contrail cover value is estimated to be uncertain by a factor of about 2. Hence, the given amount of radiative forcing by contrails is uncertain by a factor of about 5, mainly because of uncertain contrail cover and optical depth values.

The computational results are fully consistent with the observed negative daytime forcing at the surface. A reduction of solar flux by an order 50  $\text{W m}^{-2}$ , as measured by Sassen (1997), is to be expected for thick contrails ( $\tau > 1$ ). The surface LW forcing is small because of shielding of terrestrial radiation by water vapor in the atmosphere above the surface. Hence, the Earth's surface gets locally cooled in the shadow of contrails (Sassen, 1997). This does not exclude a warming of the whole atmosphere-surface system driven by the net flux change at the TOA. As shown, for example, by radiation-convection models, vertical heat exchange in

the atmosphere may cause a warming of the surface even when it gets less energy by radiation (Strauss *et al.*, 1997). The measurements of Kuhn (1970) show strongly reduced downward SW fluxes below contrails which are not balanced by a similar increase in downward LW fluxes. This might be a consequence of the narrow geometry of contrails. A strong localized SW cooling in the shadow of contrails may be balanced by the integral change of less focused LW radiation. The 3-D effect of narrow but thick contrails has not yet been computed.

### 5.3 Indirect effect due to change in particle size

Aircraft emissions may have indirect effects on radiative forcing, e.g., by changing the particle size spectra in otherwise existing ‘natural’ cirrus clouds. Some measurements indicate that aircraft emissions may induce a factor of 2 to 3 more but smaller ice particles in cirrus clouds (Ström and Ohlsson, 1998b), regionally. Hence, aircraft may increase the optical depth of natural cirrus clouds. Therefore, the sensitivity of radiative forcing to changes in the particle size is of particular interest. For thin cirrus with few small particles, additional smaller particles tend to cause stronger heating by increasing cloud albedo less strongly than emissivity (Fu and Liou, 1993). However, contrails may contain very small particles of 1 to 10  $\mu\text{m}$  radius. Such small particles have low absorption efficiency but larger single scattering albedo, causing more scattering and less absorption per unit mass, in particular, at infrared wavelengths. Hence, in this size range, a reduction of particle size increases the system albedo much more than the emissivity and hence causes a cooling at least for sufficiently large IWP values.

As shown in Fig. 6, for fixed IWC, smaller particles increase both the SW and the LW forcing. As a consequence, the net forcing increases with smaller particles or larger optical depth also but less strongly. This result holds only as long as the contrail is optically thin, see Fig. 3. For optically thick cirrus the increase in optical depth causes a reduction of net radiative forcing. Most natural cirrus is optically thin suggesting that the warming effect prevails. Figure 7 shows that the sensitivity of net forcing to a change in particle radius for the given IWP values is slightly larger in the present computation than in the results of Fortuin *et al.* (1995) and amounts to about

$$\Delta F_{\text{net}}/\Delta r = -1 \text{ W m}^{-2} \mu\text{m}^{-1}.$$

Consistent with the results presented by Fortuin *et al.* (1995) and Wyser and Ström (1998), the sensitivity is positive for small and negative for larger particles. As shown by the results of Fortuin *et al.* (1995), the critical radius increases from about 5 to 10  $\mu\text{m}$  with IWP value and the sensitivity to particle changes reaches its maximum for 10 to 20  $\text{g m}^{-2}$  IWP and 20 to 40  $\mu\text{m}$  effective particle radius (optical depth of order 1), which is in the range to be expected for high altitude thin cirrus clouds.

An increase in particle number by a factor of 2 would imply particles smaller by a factor of  $2^{-1/3}$  or 26%. For a

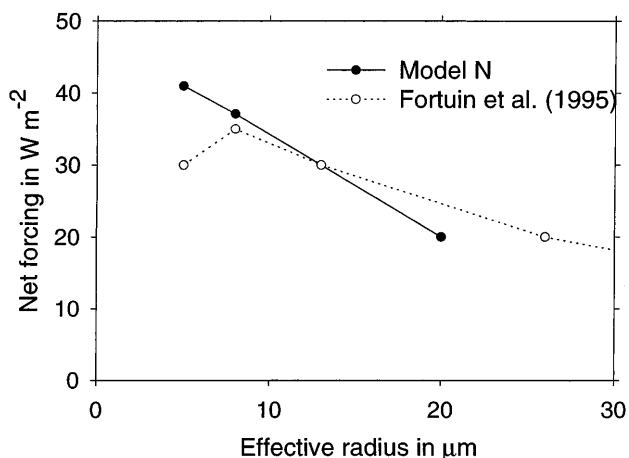


Fig. 7. Net forcing versus effective particle radius for fixed ice water path (IWP) and for 100% contrail cover with parameters as in case (a). Results from the present computations (model N, solid curve with solid dots), results from Fortuin *et al.* (1995) for IWP = 4  $\text{g m}^{-2}$  (dashed curve with open symbols)

mean radius of, e.g., 30  $\mu\text{m}$  in a cirrus cloud, this implies an increase in net forcing of about  $5 \text{ W m}^{-2}$  for 100% cirrus cover. The global cirrus cover is of order 30%. In a heavy air traffic region over Germany, Ström and Ohlsson (1998) estimate that aircraft may impact 25% of cirrus clouds. Based on the ratio of global to European contrail cover (Sausen *et al.*, 1998), the global fraction of impacted cirrus clouds is probably more than an order of 10 times smaller. Hence, aircraft may affect up to 2.5% of all cirrus clouds, and the global radiative forcing due to an increase in particle number could reach an order  $0.04 \text{ W m}^{-2}$  globally. It suggests that the indirect effect by particle changes might be comparable in magnitude to the direct effect.

## 6 Conclusions

Major parameters influencing static radiative forcing due to contrails were identified from a model study. Contrails were considered as geometrically and optically thin plane parallel homogeneous cirrus layers in a static atmosphere. The ice water content depends on the amount of water available for ice particle formation in ice-supersaturated air, implying contrails to be thinner at higher levels with lower ambient temperatures. The model atmospheres include tropical, mid-latitude, and subarctic summer and winter atmospheres, where aircraft fly. Three state-of-the-art radiative transfer models are applied. The differences between the model results are small and do not influence the conclusions. Three-dimensional geometry and climate feedback effects are not included in this study.

The radiative forcing of contrails is similar to that by thin cirrus clouds. A temporally constant cover by optically thin contrails increases the net radiative heat budget below the top of the atmosphere but cools radiatively at the Earth's surface. The radiative forcing grows with the optical depth and the amount of contrail



cover. The negative net forcing values computed by Fortuin *et al.* (1995) apply to cirrus clouds with optical depth values that are larger than expected for contrails. Contrails heat most when covering a warm and bright surface. Contrails are most efficient in radiatively forcing the Earth's atmosphere in the tropics and above low-level clouds. Contrails with smaller ice particles cause stronger heating, unless the mean particle radius is smaller than about 5  $\mu\text{m}$  (depending on IWP). Cirrus with smaller particles cause stronger heating only when optically thin. Aircraft emissions may cause indirect climate forcing by changing the particle size of natural cirrus clouds. This indirect forcing may be comparable to the direct forcing due to additional contrail cloud cover. The indirect effects due to additional cirrus forming from aged aircraft aerosol or changes due to enhanced precipitation from modified cirrus are unknown. Contrails cool the surface radiatively during the day and heat the surface during the night, and hence reduce the daily temperature amplitude. The net effect depends strongly on the daily variation of contrail cloud cover. For a global mean contrail cover of 0.1% and an average optical depth of 0.2 to 0.5, contrails cause about 0.01 to 0.03  $\text{Wm}^{-2}$  daily and annual mean instantaneous radiative forcing. This is of the same order of magnitude as the radiative forcing due to all previous carbon dioxide emissions by aviation. The best estimate value 0.02  $\text{Wm}^{-2}$  of global contrail forcing is uncertain to about a factor 5, mainly because of not well known contrail cover and optical depth values.

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